## Applications of Sea Level Measurements to Surveying

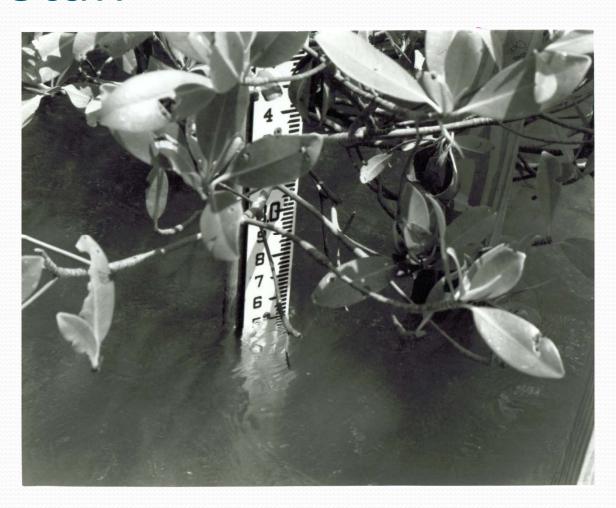
Dr. George Cole

## Applications of Sea Level Measurements to Surveying

- 1. Instrumentation for Measurements
- 2. Datum Control
- 3. Sources of Sea Level Data
- 4. Tidal Datums
- 5. Applications to Hydrographic Surveys
- 6. Applications to Boundaries
- 7. Analysis of Sea Level Trends

# 1. Instruments forSea Level Measurements

## Tide Staff



Stilling Well with Graphic Recorder

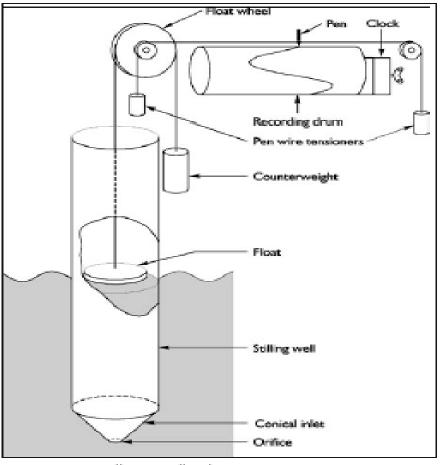
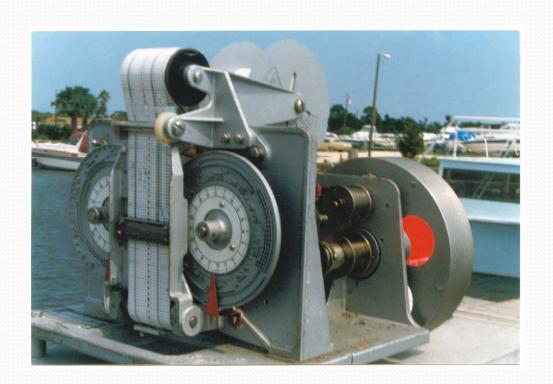


Figure 3.1 Stilling well tide gauge.

## **ADR Gauge**



## Typical Pressure Gauge



Installed pressure gauge



## **Bubbler Pressure Gauge**

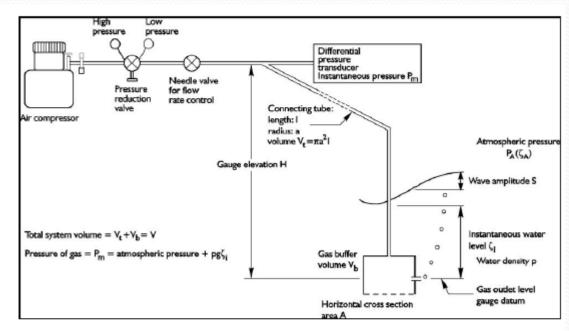


Figure 3.2 Bubbler pressure gauge.

## Reflection Type Gauges

- Acoustic gauges (use sound to measure varying distance to surface of water from a fixed point above)
- Radar gauges (uses radar for measurements to water surface)

## Typical Modern NOAA Tide Station with Acoustic Gauge

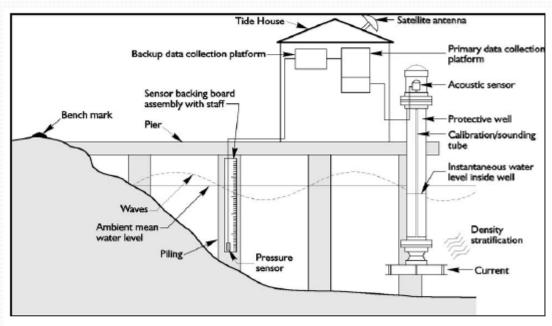


Figure 3.5 NGWLMS tide gauge.

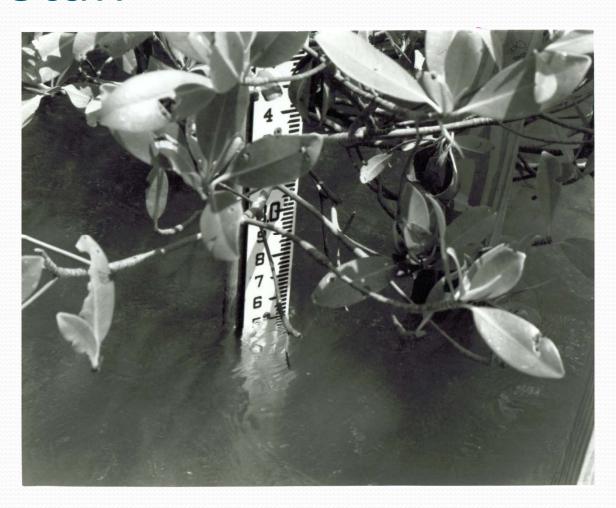
## Typical Modern NOAA Tide Station with Acoustic Gauge



## Control Box for Acoustic Gauge



## Tide Staff



#### 2. Datum Control

### **Datum Control & Leveling**

• Sea level measurements are meaningless for most applications unless related to a stable fixed surface.

### **Datum Control & Leveling**

- Typically, datum control is accomplished by relating observations to a land bench mark
- Since it is poor practice to depend on a single BM, usually at least 5 BMs are used.

### Tidal Bench Mark



## High Precision Leveling

(digital level with precision of 0.3mm/km)



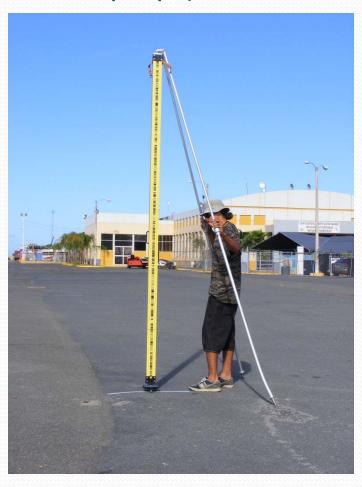
### High Precision Leveling

(fixed leg tripod with temperature sensors at 2 heights)



## High Precision Leveling

(one-piece invar rods with props)



#### To avoid or detect local subsidence

- 1. Use of bedrock, large foundation, or deep rod marks
- 2. Location of BMs
- 3. Frequent releveling
- 4. Ties to geodetic network
- 5. Continuous GPS observations
- 6. Gravity observations

## 3. Sources of Sea Level Data

### **Two Primary Sources**

• www.tidesandcurrents.noaa.gov

National Ocean Service (NOS) of NOAA (formerly known as the U.S. Coast & Geodetic Survey)

www.pol.ac.uk/psmsl

Permanent Service for Mean Sea Level (PSMSL) - international data base

#### **PSMSL** Web Site

• Data for this site is from over 2000 sites contributed by various government agencies in various nations. Longest record in the data base is from Brest, France which began in 1806.

#### **PSMSE** Web Site

- Best site for Monthly or annual average sea level data
- Data is typically in mm and is adjusted to a common datum (revised local reference)

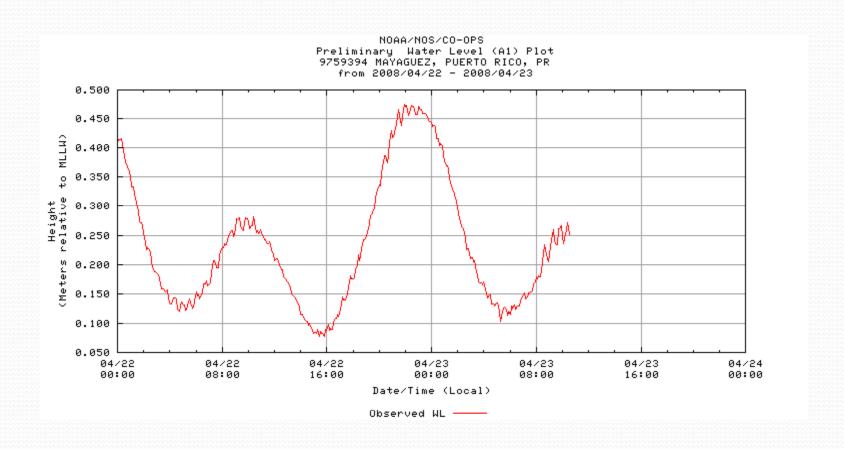
#### **NOAA** Web Site

- Best site for higher frequency observations
- Currently has large network of real-time tide stations
- Also has large data base of historic observations as well as information of tidal datums calculated for various stations that are monumented with bench marks

#### Active (Real-Time) Stations for Puerto Rico

- Culebra
- Vieques Island
- San Juan
- Magueyes Island
- Mayaguez
- Aguadilla
- Mona Island
- (Others coming soon)

## Active Stations near real time data



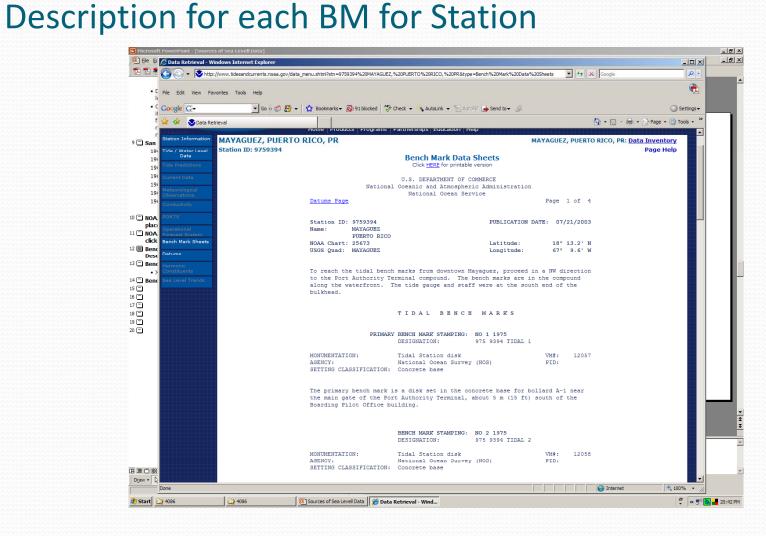
### **Historic Data**

#### **Historic Tide Data**

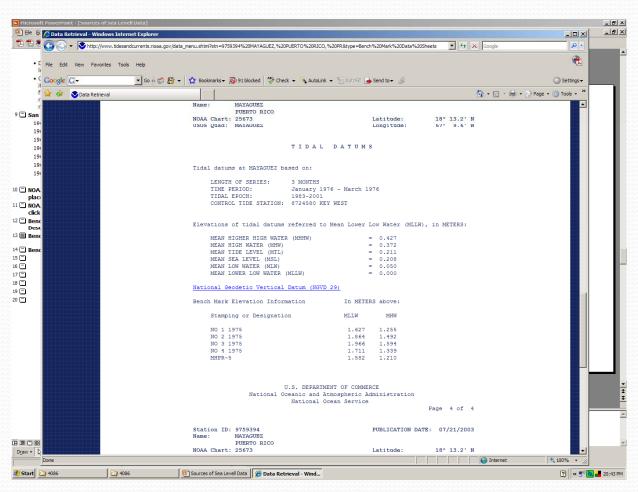
Station:	Magueyes	Island,	PR

Date	Time	Predicted	Observed
20071230	00:00	0.28	0.42
20071230	00:06	0.28	0.42
20071230	00:12	0.27	0.43
20071230	00:18	0.27	0.45
20071230	00:24	0.27	0.44

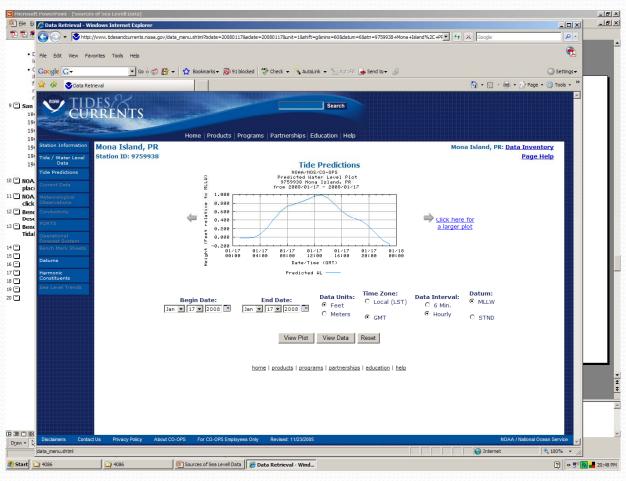
## Bench Mark Sheet



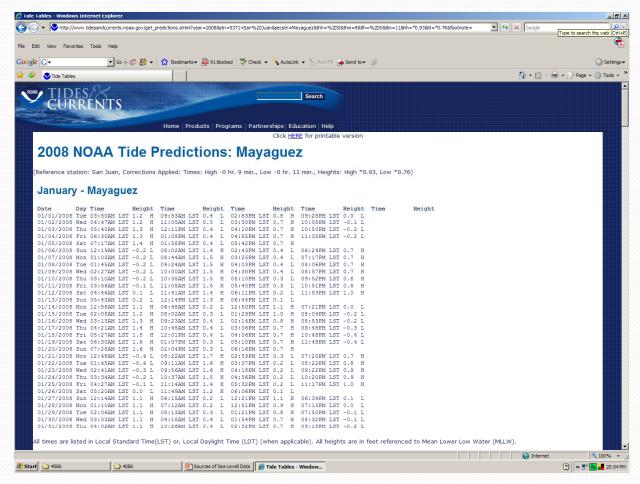
## Bench Mark Sheet Tidal Elevations for Bench Marks



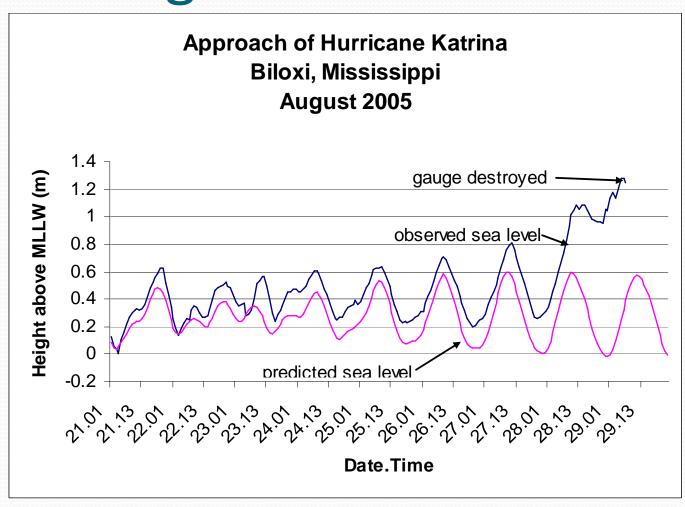
## Graphic Predictions (only active stations)



## High/Low Tide Predictions (all stations)



## Storm Surge

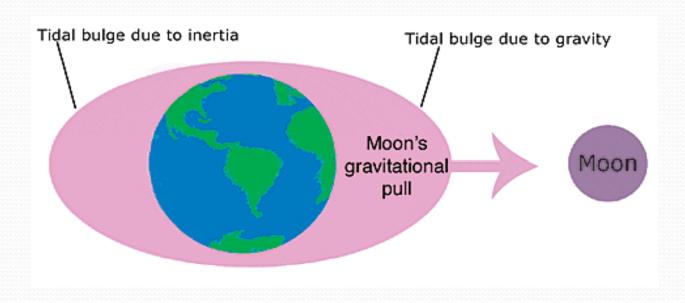


## 4. Tidal Datums

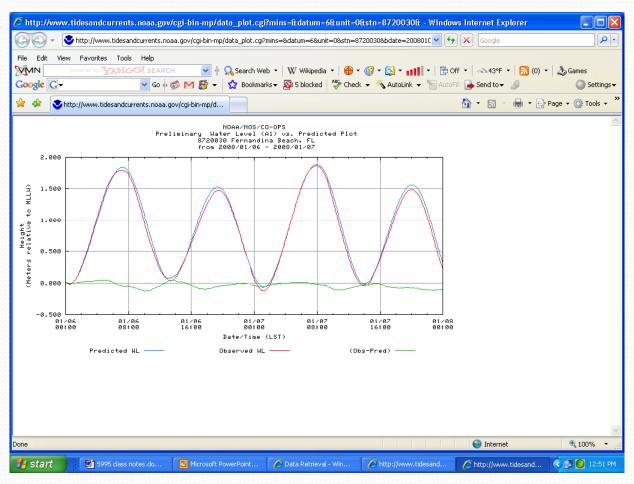
#### Cause of Tides

- Tides caused by gravitation attraction of moon & sun
- The force creates a "bulge" in the water below those bodies and at 180 degrees.
- The bulges may be considered as constituent sine waves

## O1 constituent (1.076 days) M2 constituent (0.518 days)



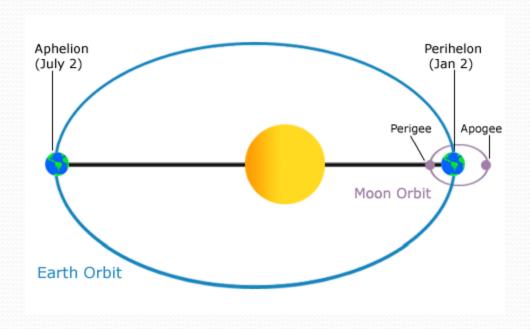
## Semi-Diurnal Tide (M2 predominates)



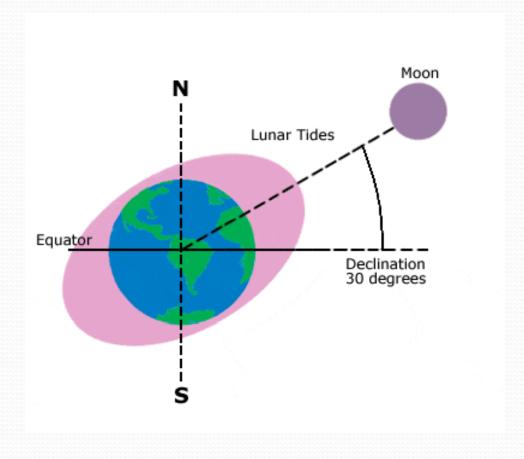
• Sun has similar, although less, effect

- S1 constituent (1.000 days)
- S2 constituent (0.500 days

#### Effect of proximity of earth to moon and sun



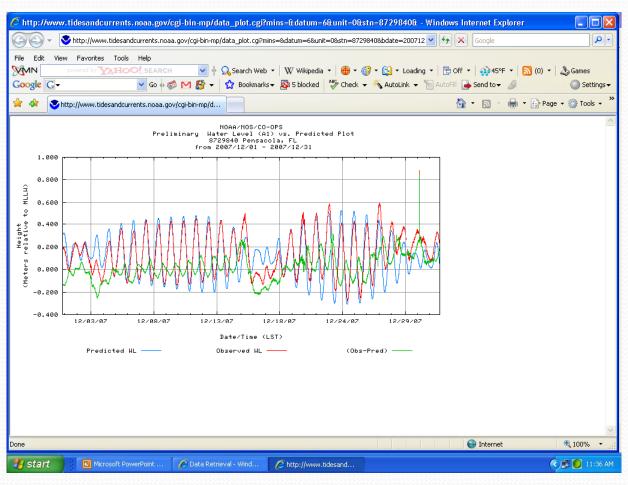
#### Effect of declination



## **Spring Tides**



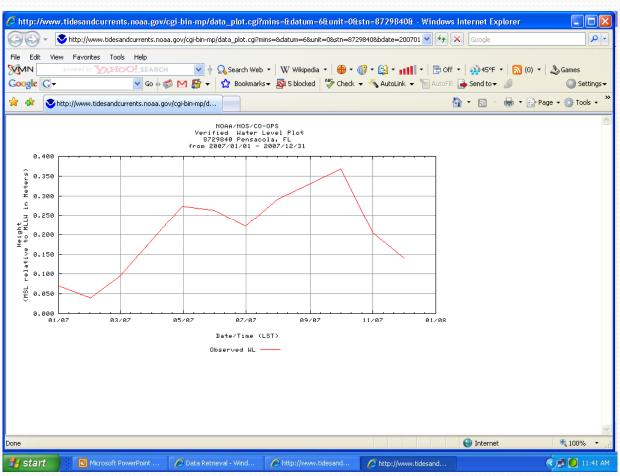
## Tides Monthly Cycles



#### **Tides**

#### Annual & Semi-Annual Cycles

Ssa constituent (182.70 days) Sa constituent (364.96 day)

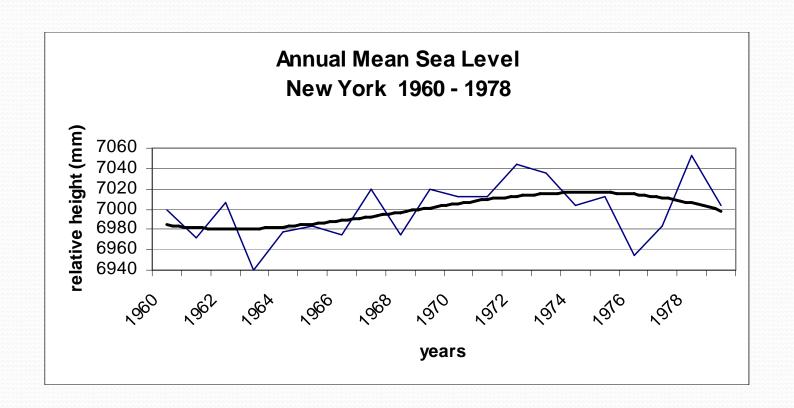


### Regression of moon's nodes

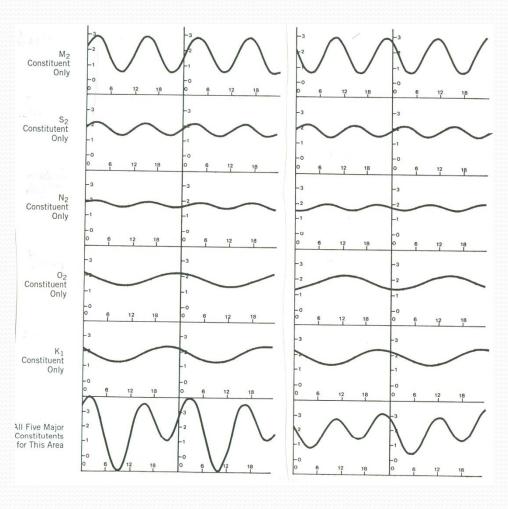
• 18.6 years

• Therefore a tidal epoch is considered to be 19 years

#### Tides 18.6 year cycle



## Summation of Tidal Constituents into Observed Tide



#### **Prediction of Tides**

• Knowledge of attributes (amplitude & phase) of the tidal constituents for a specific area allows the prediction of tides for that area.

#### **Prediction of Tides**

$$h = H_o + \sum_{i=1}^{37} f_i H_i \cos[a_i t + (V_o + u) - \kappa_i]$$

Where  $H_0$  = mean height of water level above prediction datum

 $H_i$  = mean amplitude of constituent i

 $a_i$  = speed of constituent i

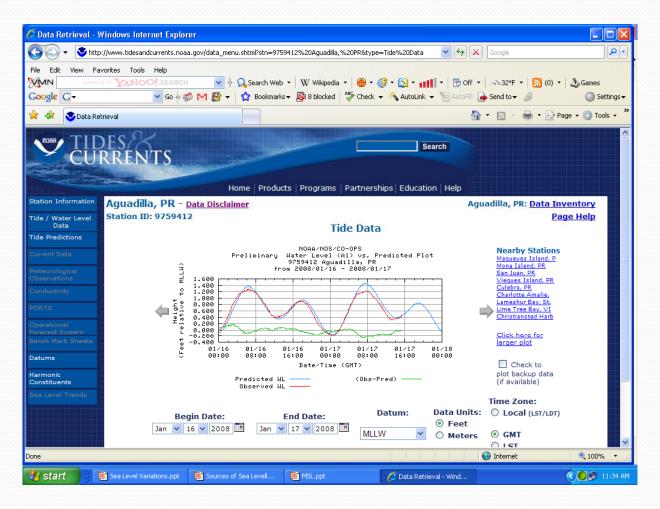
 $f_i$  = factor for reducing  $H_i$  to prediction year

 $(V_o + u) = equilibrium argument of constituent i at time t$ 

 $\kappa_i$  = phase angle of constituent i

t = time reckoned from beginning of prediction year

#### **Tidal Predictions**



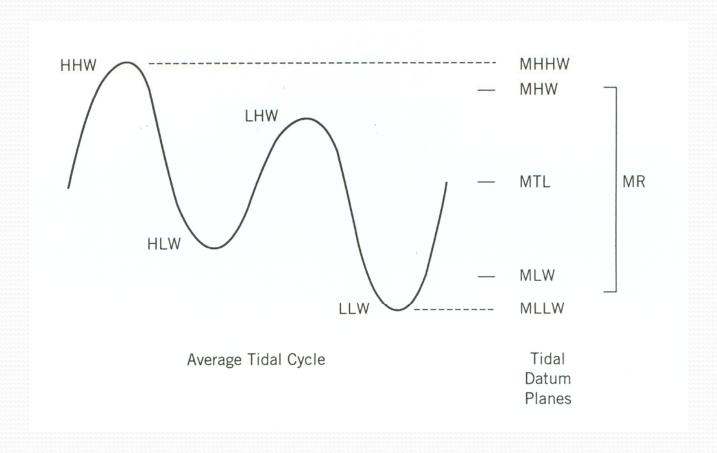
#### **Tidal Datum**

• Definition: average of a specific tidal extreme over a 19-year tidal epoch

• Examples: MHW

**MLW** 

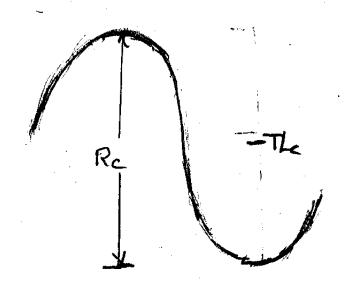
#### **Tidal Datum Planes**



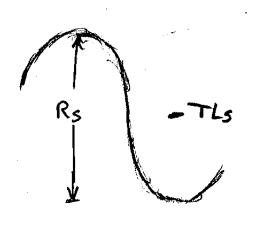
#### **Tidal Datums**

• When 19-years of observations not available, the equivalent of a 19-year mean tidal datum may be determined using a shorter period of observations by use of simultaneous comparison with another tide station where a 19-year mean value is known.

## Standard Method of Calculation (Range-Ratio Method)



Control Station (c)



Subordinate Station (5)

### 1. Determine Mean Range

$$\frac{MR_S}{R_S} = \frac{MR_C}{R_C}$$

Therefore

$$MR_S = \frac{R_S}{R_C} MR_C$$

Where

MR = 19-year mean range

R = observed range

MTL = 19-year mean tide level

TL = observed mean tide level

c = subscript denoting control station

s = subscript denoting subordinate station

#### 2. Determine Mean Tide Level

$$MTL_S - TL_S = MTL_C - TL_C$$

- Therefore  $MTL_S = MTL_C TL_C + TL_S$
- Where MR = 19-year mean range

R = Observed Range

MTL = 19-year mean tide level

TL = observed mean tide level

c = subscript denoting control station

s = subscript denoting subordinate station

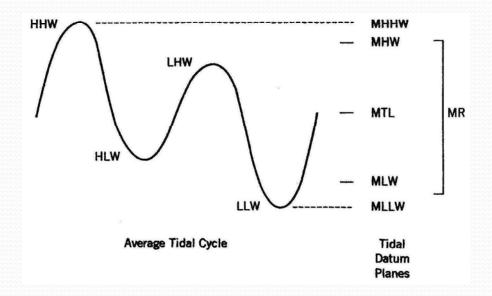
#### 3. Determine MHW or MLW

$$MHW_S = MTL_S + \frac{MR_S}{2}$$

$$MLW_S = MTL_S - \frac{MR_S}{2}$$

#### MHHW & MLLW

DHQ = Diurnal High Water Inequality = MHHW – MHW DLQ = Diurnal Low Water Inequality = MLW - MLLW



#### **MHHW**

- DHQ = <u>observed</u> diurnal high water inequality
   = HHW HW
- MDHQ = <u>19-year mean</u> diurnal high water inequality
   = MHHW MHW

$$MDHQ_S = \frac{(DHQ_S)(MDHQ_C)}{DHQ_C}$$

$$MHHW = MHW + MDHQ$$

#### **MLLW**

- DLQ = <u>observed</u> diurnal low water inequality
   = LW LLW
- MDLQ = 19-year mean diurnal low water inequality
   MLW MLLW

$$MDLQ_S = \frac{(DLQ_S)(MDLQ_C)}{DLQ_C}$$

$$MLLW = MLW - MDLQ$$

#### Local Variation in MSL

- Water salinity
- Water temperature
- Sub surface hydrography

### Variation in Tidal Range

#### Three Major Causes

- Due to conservation of mass, shoaling water or narrowing channel increases tidal range, deepening water or widening of channel decreases tidal range
- Reflected tidal waves can increase & decrease range (resonance)
- Coriolis effect

#### **Conservation of Mass**

 Due to conservation of mass, shoaling water or narrowing channel increases tidal range, deepening water or widening of channel decreases tidal range

#### Resonance

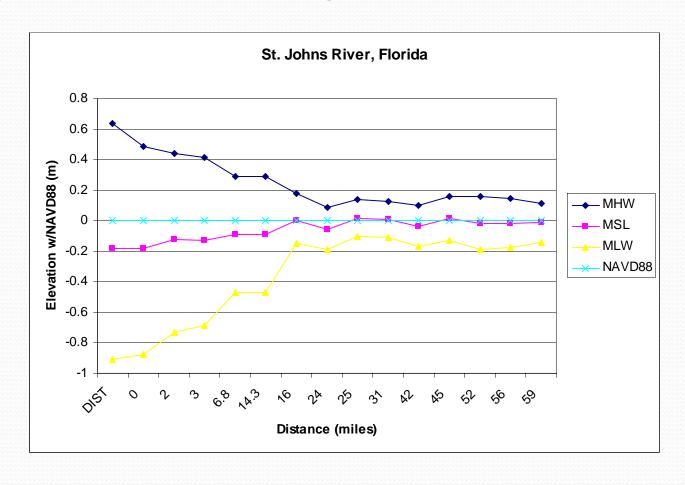
- At the point where the reflected wave and the direct wave are "in phase", maximum ranges occur (1/2 wave length)
- Where they are "out of phase", minimum ranges occur (1/4 & 3/4 wave lengths)
- Wave lengths can be calculated as the product of the average speed of the tidal wave in the estuary and the tidal period of 12.42 hours.

#### **Coriolis Effect**

• Coriolis effect causes a right-hand veer to current flow. This results in piling up of water on the right side of estuary on the incoming tide and a lowering on that side with the outgoing tide – thus greater range.

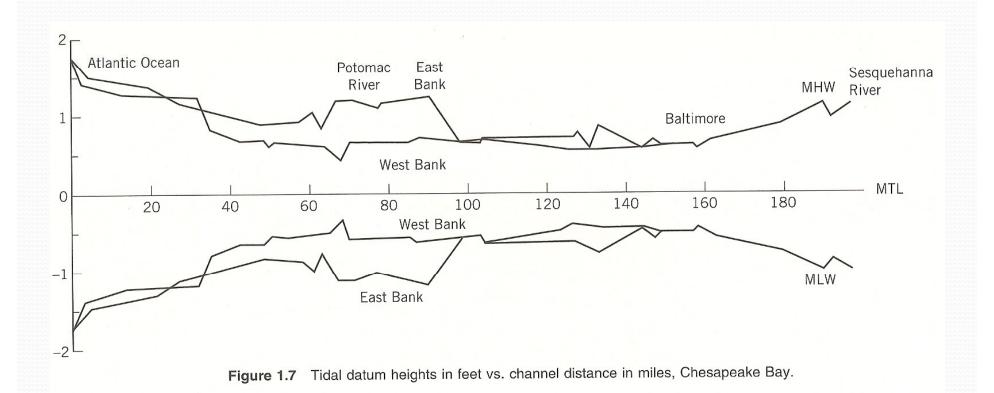
#### St Johns River

(example of effects of widening channel)



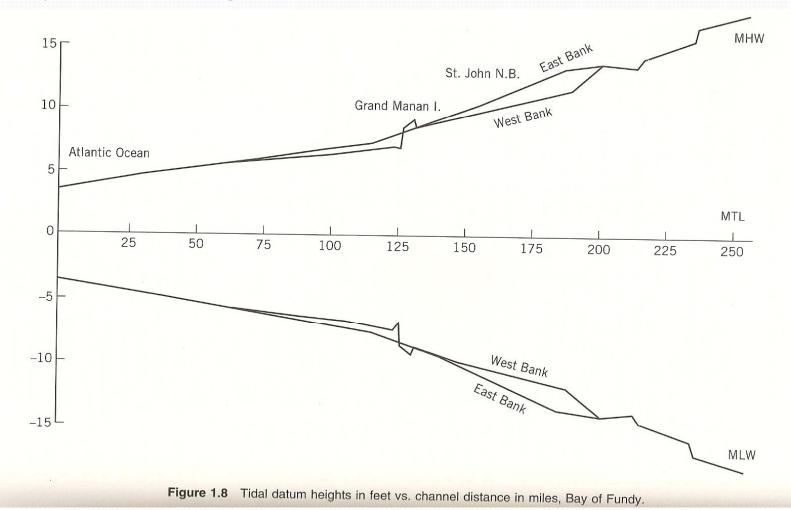
### Chesapeake Bay

(example of resonance & Coriolis effect)



### Bay of Fundy

(example of shoaling water & resonance)



#### Impact of Variations on Surveying

- A tidal datum is valid only in the immediate area in which is was determined.
- When a tidal datum is needed in other areas, a new local datum must be determined
- When deciding when new stations are needed and where they should be placed, an understanding of the causes of tidal variations is essential!

# 5. Applications to Hydrographic Surveys

#### Vertical Datum Correction

 Although corrections for varying velocity of sound and the draft of the boat must also be made, pertinent to this seminar is the vertical datum correction. That correction reduces the sounding to a common datum of reference such as MLLW or NAVD.

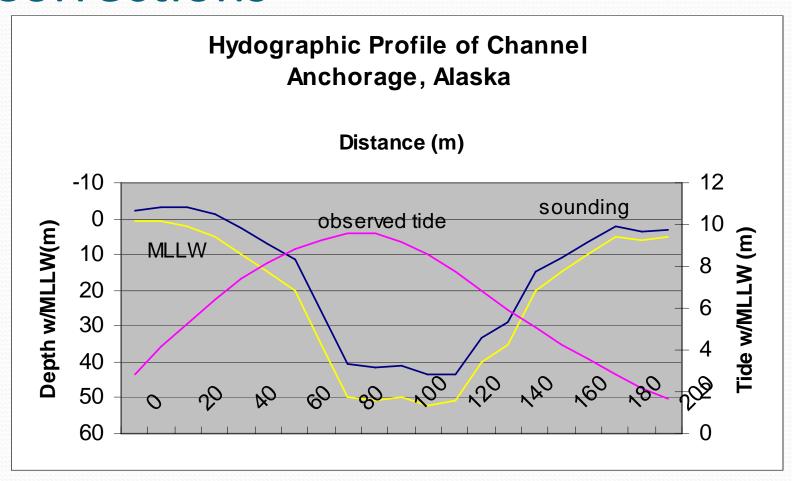
#### **Vertical Datums**

- Traditionally, topo surveys on land have been referenced to a geodetic datum such as NAVD which approximates MSL.
- Traditionally, hydro surveys have been referenced to a local tidal datum, such as MLLW, to provide conservative soundings for navigation.

#### Datum Corrections for Hydrography

- The traditional process for determining a vertical datum correction is to operate a separate tide station in the area whenever a hydrographic survey is in progress.
- Data from that gauge is used to correct the soundings to the desired datum.

# Application of Vertical Datum Corrections



# 6. Applications to Coastal Boundaries

#### **Public Trust Doctrine**

- <u>Public trust doctrine</u>: Individual nations or states hold title on behalf of the public to the submerged lands under navigable waters within their respective boundaries.
- First stated in the Roman Civil Code of Emperor Justinian I (500 AD) The sea as well as rivers are res communes or commonly owned by all mankind.

#### **Coastal Boundaries**

 Coastal boundaries serve as the division line between waters of the public trust and uplands subject to private ownership. They have become even more important in recent times with the intense development along most coastlines and with concerns with protection of the environment.

#### **Coastal Boundaries**

- As a result, there is a demand for precise location of coastal boundaries.
- BUT, since the line between the upland and the sea moves with each wave and with each tidal cycle, the precise location of a coastal boundary has to involve more than calling it the "edge of the sea"

#### **Coastal Boundaries**

• Various definitions allowing a more precise definition of coastal boundaries have evolved in different areas of the world.

 Due to the large daily range of tides in the British Isles, coastal boundaries are based on the daily tides. That system uses the average reach of the daily tide – the mean high water line

• Probably the earliest mention of using tides to determine the coastal boundary was in a book by Thomas Diggs (a <u>surveyor</u>, engineer & lawyer) entitled "Proofs of the Queen's Interest in Land left by the Sea and the Salt Shores Thereof" (late 1400s)

- A couple of hundred years later (1666), Lord Chief Justice Matthew Hale, in a book entitled *De Jure Maris*, wrote that the foreshore (the area which is overflowed by "ordinary tides or neap tides, which happen between the full and change of the moon"), belong to the crown
- A latter British case (1854) ruled that the boundary was to be found by "the average of medium tides in each quarter of a lunar evolution during the year"

• In view of the definition of the mean high tide...and the further observation that ... there should be "a periodic variation in the rise of water above sea level having a period of 18.6 years" ... in order to ascertain the mean high tide line with requisite certainty... "an average of 18.6 years should be determined as near as possible" (Borax Consolidated v City of Los Angeles, 1935)

- Most US coastal states have followed the Anglo/American Common Law and consider the mean high water line, as defined in the Borax case, to be the boundary (There are exceptions in several "low water" states)
- As may be seen from its definition, the MHW line represents an attempt to use the <u>average of the</u> <u>daily reach of the waters</u> as the boundary.

 So ... under the Anglo/American Common Law, how does a surveyor go about surveying a coastal boundary?

- Survey Process
- 1. Determine local tidal datum
  - a. Look for NOAA Bench Marks for closest station
  - b. If station is in the immediate area, it may be used directly. Otherwise, a new local datum must be established by the process of <u>simultaneous comparison</u>.
  - c. That process involves having a tide gauge at a station where a tidal datum is known and another at the survey site. Length of observations needed would vary with distance between sites.

- Survey Process (Continued)
  - 1. Determine local elevation of mean high water (Continued)
  - d. The <u>simultaneous comparison</u> process involves calculating a datum using the range ratio formulas
  - 2. Locate the MHW <u>line</u>
  - a. Usual process is to level from the tidal bench marks and follow the contour of the local elevation of MHW.
  - b. An alternate process is to watch a tide staff during an incoming tide and stake the leading edge of the water when it reaches MHW.

# Benchmark Sheet for Isla Magueyes

Bench Mark Elevations

	BN	<b>I</b>	MLW	MHW
9110	В	1980	3.183	2.982
9110	D	1980	0.671	0.470
9110	E	1980	0.937	0.736
9110	F	1982	1.746	1.545
9110	G	1982	3.244	3.042
9110	Н	1998	3.019	2.818

# Benchmark Sheet for Isla Magueyes

```
Tidal datums based on 19 Years
  TIDAL EPOCH: 1983-2001
  Highest 09/22/1998) = 0.690
  WHHM
                       = 0.204
                       = 0.201
  MHW
                       = 0.102
  MTL
                       = 0.101
  MSL
                       = 0.003
  MLW
                       = 0.000
  MLLW
  Lowest (06/11/1968) = -0.268
```

#### II. Roman Civil Law

- In areas where the land title has its roots in a grant from a sovereign power where law derived from the ancient Roman Civil Code prevailed, different rules generally exist.
- Since that law was developed in an area with minimal daily tidal range, it does not define the coastal boundary in terms of daily tide, but in terms of seasonal water level changes.

- Roman Civil Law based on the 500 BC Roman Code:
- Thus, the following things are by natural law common to all the air, running water, the sea, and consequently the sea-shore.
- The sea-shore, that is, the shore as far as the waves go at furthest, was considered to be-long to all men...... The sea shore extends as far as the greatest winter floods runs up

• Old Spanish law, Las Siete Partidas, written in the thirteenth century, contained similar language and defines the sea shore as follows (Partida 3, Title 28, Law 4):

... e todo aquel lugar es llamado ribera de la mar quanto se cubre el agua della, quanto mas crece en todo el ano, quier en tiempo del invierno o verano...

• U.S. Case law (Borax Consolidated v City of Los Angeles) clearly distinguishes between the Anglo/American common law and the civil law:

By the civil law, the shore extends as far as the highest waves reach in winter. But by the common law, the shore "is confined to the flux and reflux of the sea at ordinary tides."

• So...how does a surveyor find the highest reach of the water????

One possibility is to use sea level measurements

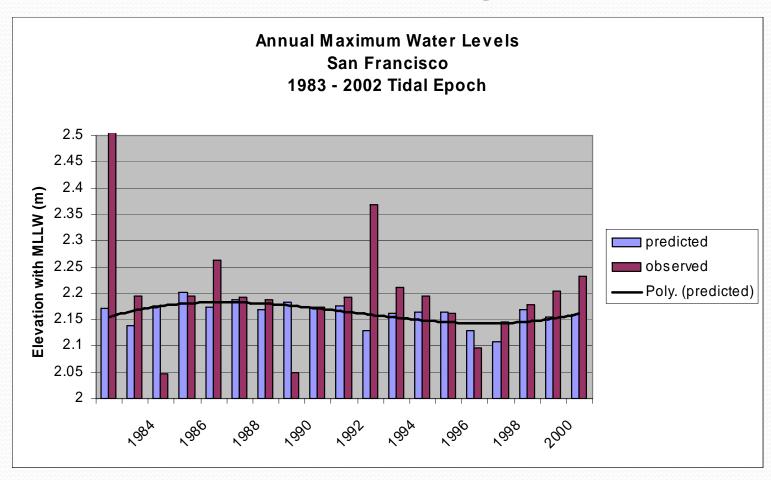
#### **Extreme Tides**

- Spring Tides
- Perigean Spring Tides
- Equinoxial Spring Tides
- Perigean-Equinoxial Spring Tides
- Highest Astronomic Tide

#### **Datums for Tidal Extremes**

- Since extreme tidal events occur infrequently, they are usually determined by predictions based on constituents derived from sea level observations rather than through direct averaging of sea level observations.
- Due to extreme weather effects, actual extreme events may differ from predicted

#### Prediction of Maximum High Water



### Tidal Datum Elevations (m) Isla Magueyes 1983 - 2001

HIGHEST OBSERVED WATER	0.690
HIGHEST PREDICTED TIDE	0.330
MHHW	0.204

MHW 0.201

MTL 0.102

MSL 0.101

MLW 0.003

MLLW 0.000

 Can sea level observations be used for coastal boundaries in Puerto Rico and if so, how should they be used?

• Let's look at prevailing administrative and legal guidance:

#### Puerto Rico

- Puerto Rico laws generally are based on the Roman Civil Code as reflected in early Spanish law:
- ... e todo aquel lugar es llamado ribera de la mar quanto se cubre el agua della, quanto mas crece en todo el ano, quier en tiempo del invierno o verano...

# Section 3.2.1.a (2), <u>Manual de Procedimientos para el Deslinde</u> del Limite Interior Tierra Adentro de los Bienes de Dominio

#### Publico Maritimo Terrestre, DRNA, 1999

"El Ciclo Metódico (también conocido como Ciclo Cronol Lunar) es un período de tiempo durante el cual las posiciones del sol, la luna y la tierra obedecen a un patrón que se repite cada 19 años. Durante un corte período de cada uno de estos ciclos lunares se produce una FGR máxima que causa a su vez que la pleamar alcance el nivel máximo posible. A este nivel del mar se le denomina como la pleamar m"Axima viva equinoccial ("highest water level"). Esta pleamar es la que causa la máxima penetración tierra adentro de las aguas marinas por los efectos mareales."

# Section 3.2.1.a (2), Manual de Procedimientos para el Deslinde del Limite Interior Tierra Adentro de los Bienes de Dominio Publico Maritimo Terrestre, DRNA, 1999

 "Para determinar el alcance tierra adentro del criterio mareal se pueden utilizar los indicadores bióticos o el alcance de la pleamar máxima viva equinoccial...." Appendix B, Manual de Procedimientos para el Deslinde del Limite Interior Tierra Adentro de los Bienes de Dominio Publico Maritimo Terrestre, DRNA, 1999

"En Puerto Rico, la LITA (límite interior tierra adentro) de los bienes de dominio públicos de la ZMT (zona marítimo-terrestre) es la línea de la pleamar máxima viva equinoccial (PMVE) en los sistemas mareales en donde é'sta supera el alcance de los mayores olas en los temporales."

Tous, José. El Límite Interior Terrestre de la Zona Marítimo-Terrestre: ¿Dónde se Tira la Línea?. Colegio de Abogados de Puerto Rico.

"En Rubert Armstrong v. E.L.A., 97 D.P.R. 588 (1969), el Tribunal Supremo de puerto Rico parece tener el mismo criterio de la ley de Costas de España, de que el limite de la zona marítimo-terrestre será el que abarque un mayor ámbito físico, hasta donde alcancen las olas en los mayores temporales o, cuando lo supere, la línea de pleamar máxima viva equinoccial."

# **Ongoing Study**

- To evaluate different methods of using sea level measurements and how they compare, a study is ongoing
- Following are some preliminary results from a survey class exercise conducted last week on Isla Magueyez

# **Ongoing Study**

• On the island, the coastal boundary was delimited last year <u>using botanical and geological indicators</u>, and the line was recently approved by the DRNA. The points on that line are marked with a series of monuments and witness posts that were located by RTK GPS.

# **Ongoing Study**

• Transects were measured at each such ZMT point and the elevations compared between the ZMT points, the highest observed water level, the highest astronomic tide and the mean high water line.

## The ZMT points were found to be above the highest observed water level



## Typical Relative Positions of the ZMT, HOT, HAT & MHW Lines



## A problem was encountered: Iguanas ate the flagging as soon as it was placed



## 7. Analysis of Sea Level Trends

## **MSL Variations**

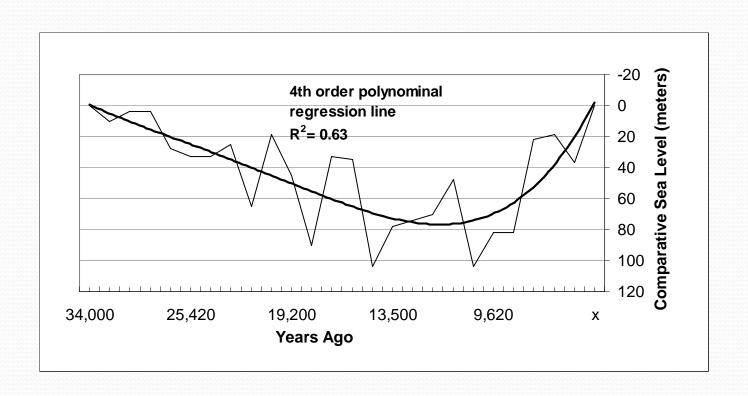
MSL: Mean of hourly heights averaged over a tidal epoch

## Temporal Variation in MSL

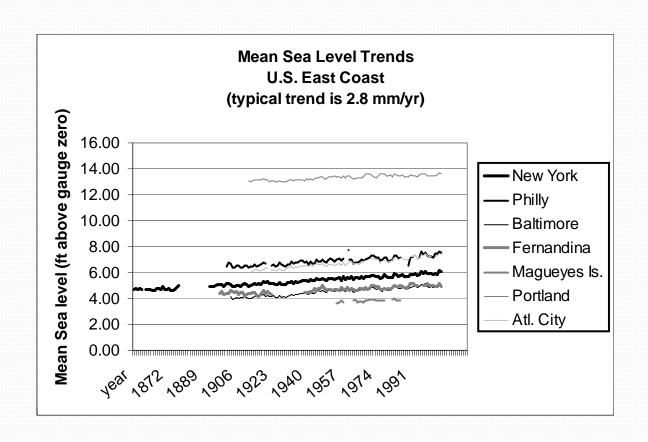
• Currently, there is great interest in variation of MSL with time, so it is important to be able to precisely measure rates of change to allow a rational approach to coastal management and engineering along the coast

• Over the short term, sea level varies considerably with the effect of the various astronomic forces reflected by the harmonic constituents. In addition, there is considerably variation due to meteorological conditions such as wind and atmospheric pressure. • Over the long term, the changes are much less rapid, but can be more significant. Such changes are associated with the continually changing trends in global climate conditions.

## Sea Levels Over Last 36,000 Years U.S. East Coast



### Typical Current Sea Level Trends

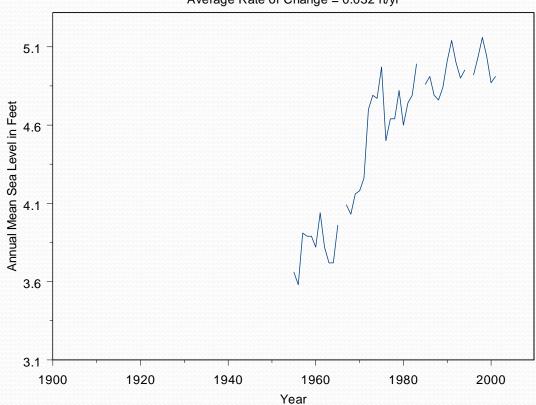


- Data from PSMSL web site may be used
- Monitoring MSL trends is complicated by local tectonic plate movement which causes a distorted view of MSL change when using sea level measurements

# Area of Rapid Sea Level Rise (10 mm/year)

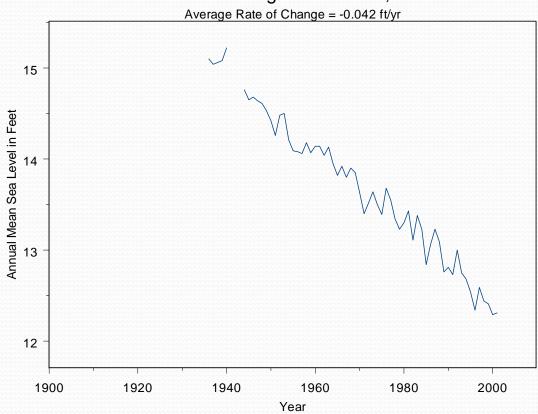
#### Sea Level Change at Freeport, Texas

Average Rate of Change = 0.032 ft/yr



## Area of Rapid Sea Level Drop (-13 mm/year)

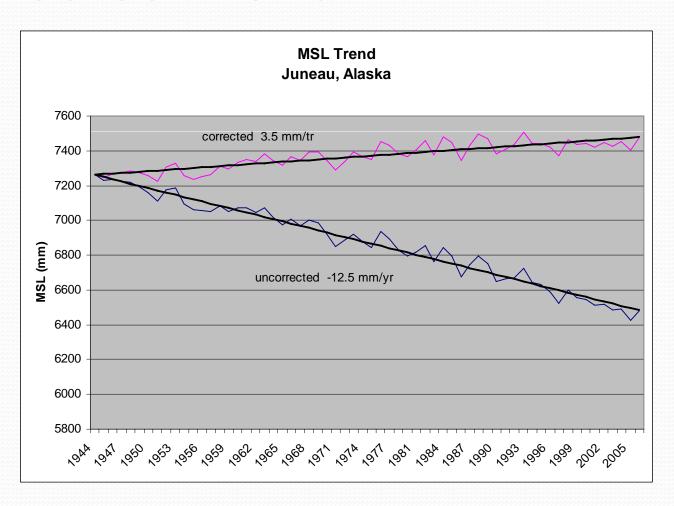
#### Sea Level Change at Jeaneau, Alaska



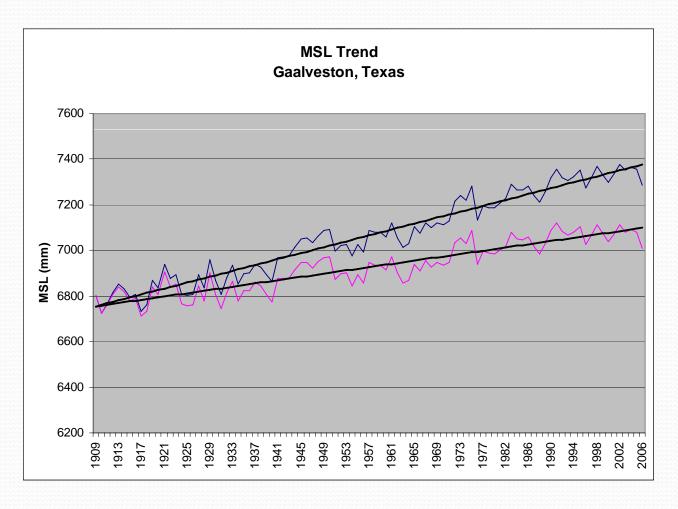
• Therefore, it is important to eliminate vertical tectonic plate movement from sea level measurements.

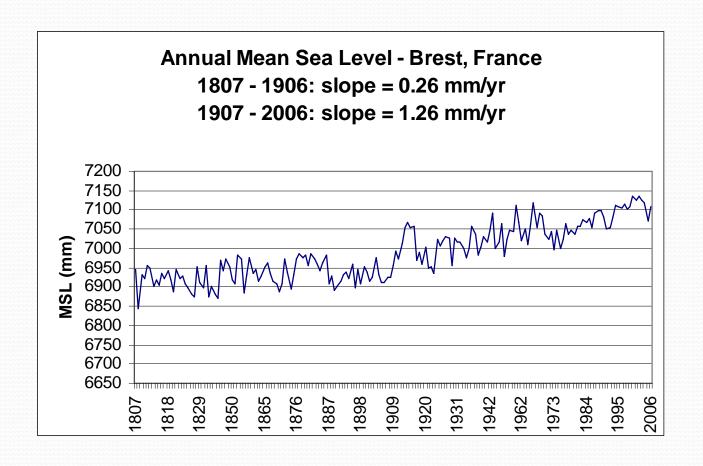
• So.... for any place where there is a long-established CORS near a tide station, you can obtain estimates of the vertical tectonic plate motion for that location from the data sheet for the CORS for use in correcting the apparent MSL changes closer to actual.

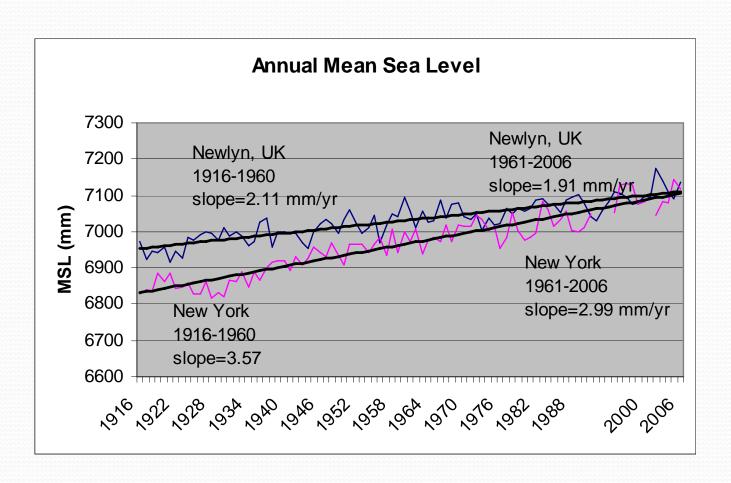
## **Corrected Trend**

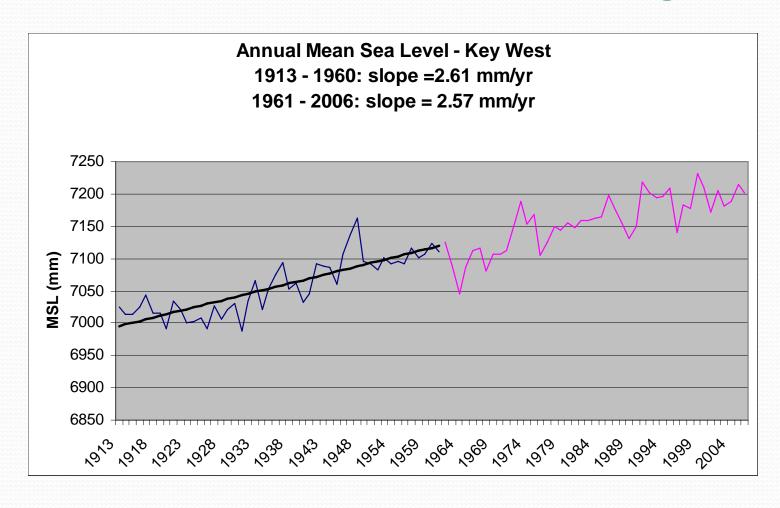


## **Corrected Trend**









- Although records are few, there was an apparent increase in rate between the 1800s and the latest century.
- However, during the latest century, there is no consistent evidence of an increase in the rate of sea level rise